

**B. E.(Common to all branches)**

**Choice Based Credit System (CBCS) and Outcome-Based Education (OBE)**

**SEMESTER - III**

TRANSFORM CALCULUS, FOURIER SERIES AND NUMERICAL TECHNIQUES			
Course Code	21MAT 31	CIE Marks	50
Teaching Hours/Week (L:T:P:S)	2:2:0:0	SEE Marks	50
Total Hours of Pedagogy	40	Total Marks	100
Credits	03	Exam Hours	03
<b>Course objectives:</b> The goal of the course Transform Calculus, Fourier series and Numerical techniques 21MAT 31 is <ul style="list-style-type: none"><li>➤ To have an insight into solving ordinary differential equations by using Laplace transform techniques</li><li>➤ Learn to use the Fourier series to represent periodical physical phenomena in engineering analysis.</li><li>➤ To enable the students to study Fourier Transforms and concepts of infinite Fourier Sine and Cosine transforms and to learn the method of solving difference equations by the z-transform method.</li><li>➤ To develop proficiency in solving ordinary and partial differential equations arising in engineering applications, using numerical methods</li></ul>			
<b>Module-1: Laplace Transform</b>			
Definition and Laplace transforms of elementary functions (statements only). Problems on Laplace's Transform of $e^{at}f(t)$ , $t^n f(t)$ , $\frac{f(t)}{t}$ . Laplace transforms of Periodic functions (statement only) and unit-step function – problems. Inverse Laplace transforms definition and problems, Convolution theorem to find the inverse Laplace transforms (without Proof) problems. Laplace transforms of derivatives, solution of differential equations. <b>(8 Hours)</b> <b>Self-study:</b> Solution of simultaneous first-order differential equations. <b>(RBT Levels: L1, L2 and L3)</b>			
Teaching-Learning Process	Chalk and talk method / PowerPoint Presentation		
<b>Module-2: Fourier Series</b>			
Introduction to infinite series, convergence and divergence. Periodic functions, Dirichlet's condition. Fourier series of periodic functions with period $2\pi$ and arbitrary period. Half range Fourier series. Practical harmonic analysis. <b>(8 Hours)</b> <b>Self-study:</b> Convergence of series by D'Alembert's Ratio test and, Cauchy's root test. <b>(RBT Levels: L1, L2 and L3)</b>			
Teaching-Learning Process	Chalk and talk method / PowerPoint Presentation		
<b>Module-3: Infinite Fourier Transforms and Z-Transforms</b>			
Infinite Fourier transforms definition, Fourier sine and cosine transforms. Inverse Fourier transforms, Inverse Fourier cosine and sine transforms. Problems. Difference equations, z-transform-definition, Standard z-transforms, Damping and shifting rules, Problems. Inverse z-transform and applications to solve difference equations. <b>(8 Hours)</b> <b>Self Study:</b> Initial value and final value theorems, problems. <b>(RBT Levels: L1, L2 and L3)</b>			
Teaching-Learning Process	Chalk and talk method / PowerPoint Presentation		

<b>Module-4: Numerical Solution of Partial Differential Equations</b>	
<p>Classifications of second-order partial differential equations, finite difference approximations to derivatives, Solution of Laplace's equation using standard five-point formula. Solution of heat equation by Schmidt explicit formula and Crank- Nicholson method, Solution of the Wave equation. Problems. (8 Hours)</p> <p><b>Self Study:</b> Solution of Poisson equations using standard five-point formula.</p> <p><b>(RBT Levels: L1, L2 and L3)</b></p>	
<b>Teaching-Learning Process</b>	Chalk and talk method / PowerPoint Presentation
<b>Module-5: Numerical Solution of Second-Order ODEs and Calculus of Variations</b>	
<p>Second-order differential equations - Runge-Kutta method and Milne's predictor and corrector method. (No derivations of formulae).</p> <p>Calculus of Variations: Functionals, Euler's equation, Problems on extremals of functional. Geodesics on a plane, Variational problems. (8 Hours)</p> <p><b>Self Study:</b> Hanging chain problem</p> <p><b>(RBT Levels: L1, L2 and L3)</b></p>	
<p><b>Course outcomes:</b> After successfully completing the course, the students will be able to :</p> <ul style="list-style-type: none"> <li>➤ To solve ordinary differential equations using Laplace transform.</li> <li>➤ Demonstrate the Fourier series to study the behaviour of periodic functions and their applications in system communications, digital signal processing and field theory.</li> <li>➤ To use Fourier transforms to analyze problems involving continuous-time signals and to apply Z-Transform techniques to solve difference equations</li> <li>➤ To solve mathematical models represented by initial or boundary value problems involving partial differential equations</li> <li>➤ Determine the extremals of functionals using calculus of variations and solve problems arising in dynamics of rigid bodies and vibrational analysis.</li> </ul>	



### Assessment Details (both CIE and SEE)

The weightage of Continuous Internal Evaluation (CIE) is 50% and for Semester End Exam (SEE) is 50%. The minimum passing mark for the CIE is 40% of the maximum marks (20 marks out of 50). A student shall be deemed to have satisfied the academic requirements and earned the credits allotted to each subject/ course if the student secures not less than 35% ( 18 Marks out of 50) in the semester-end examination(SEE), and a minimum of 40% (40 marks out of 100) in the sum total of the CIE (Continuous Internal Evaluation) and SEE (Semester End Examination) taken together

#### Continuous Internal Evaluation:

1. Three Unit Tests each of **20 Marks (duration 01 hour)**
2. First test at the end of 5<sup>th</sup> week of the semester
3. Second test at the end of the 10<sup>th</sup> week of the semester
4. Third test at the end of the 15<sup>th</sup> week of the semester

#### Two assignments each of 10 Marks

5. First assignment at the end of 4<sup>th</sup> week of the semester
6. Second assignment at the end of 9<sup>th</sup> week of the semester

Group discussion/Seminar/quiz any one of three suitably planned to attain the COs and POs for **20 Marks (duration 01 hours)**

7. At the end of the 13<sup>th</sup> week of the semester

The sum of three tests, two assignments, and quiz/seminar/group discussion will be out of 100 marks and will be **scaled down to 50 marks**

(to have less stressed CIE, the portion of the syllabus should not be common /repeated for any of the methods of the CIE. Each method of CIE should have a different syllabus portion of the course).

**CIE methods /question paper is designed to attain the different levels of Bloom's taxonomy as per the outcome defined for the course.**

#### Semester End Examination:

Theory SEE will be conducted by University as per the scheduled timetable, with common question papers for the subject **(duration 03 hours)**

- The question paper will be set for 100 marks and marks scored will be proportionally scaled down to 50 marks
- The question paper will have ten questions. Each question is set for 20 marks.
- There will be 2 questions from each module. Each of the two questions under a module (with a maximum of 3 sub-questions), **should have a mix of topics** under that module.
- The students have to answer 5 full questions, selecting one full question from each module

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**Suggested Learning Resources:****Text Books:**

1. **B.S.Grewal:** "Higher Engineering Mathematics", Khanna publishers, 44<sup>th</sup> Ed. 2018
2. **E.Kreyszig:** "Advanced Engineering Mathematics", John Wiley & Sons, 10<sup>th</sup> Ed. (Reprint), 2016.

**Reference Books**

1. **V.Ramana:** "Higher Engineering Mathematics" McGraw-Hill Education, 11<sup>th</sup> Ed.
2. **Srimanta Pal & Subodh C. Bhunia:** "Engineering Mathematics" Oxford University Press, 3<sup>rd</sup> Reprint, 2016.
3. **N.P Bali and Manish Goyal:** "A textbook of Engineering Mathematics" Laxmi Publications, Latest edition.
4. **C. Ray Wylie, Louis C. Barrett:** "Advanced Engineering Mathematics" McGraw – Hill Book Co. New York, Latested.
5. **Gupta C.B, Sing S.R and Mukesh Kumar:** "Engineering Mathematic for Semester I and II", McGraw Hill Education (India) Pvt. Ltd 2015.
6. **H.K.Dass and Er. Rajnish Verma:** "Higher Engineering Mathematics" S. Chand Publication (2014).
7. **James Stewart:** "Calculus" Cengage publications, 7<sup>th</sup> edition, 4<sup>th</sup> Reprint 2019.

**Web links and Video Lectures (e-Resources):**

- <http://ac.in/courses.php?disciplineID=111>
- [http://www.class-central.com/subject/math\(MOOCs\)](http://www.class-central.com/subject/math(MOOCs))
- <http://academicearth.org/>
- <http://www.bookstreet.in>
- VTU e-Shikshana Program
- VTU EDUSAT Program

**Activity-Based Learning (Suggested Activities in Class)/ Practical Based learning**

- Quizzes
- Assignments
- Seminars

  
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